

# REVIEW Topic 4 Introduction to Functions



## **Quick Review**

You can use graphs to represent the relationship between two variables.

## Example

A dog owner plays fetch with her dog. Sketch a graph to represent the distance between them and the time.



#### Exercises

1. **Travel** A car's speed increases as it merges onto a highway. The car travels at 65 mi/h on the highway until it slows to exit. The car then stops at three traffic lights before reaching its destination. Draw a sketch of a graph that shows the car's speed over time. Label each section.

2. **Surfing** A professional surfer paddles out past breaking waves, rides a wave, paddles back out past the breaking waves, rides another wave, and paddles back to the beach. Draw a sketch of a graph that shows the surfer's possible distance from the beach over time.



## **Quick Review**

A function is a relationship that pairs each input value with exactly one output value. A linear function is a function whose graph is a line or part of a line.

## Example

The number y of eggs left in a dozen depends on the number x of 2-egg omelets you make, as shown in the table. Represent this relationship using words, an equation, and a graph.

Number of Omelets Made, x	0	1	2	3
Number of Eggs Left, y	12	10	8	6

Look for a pattern in the table. Each time x increases by 1, y decreases by 2. The number y of eggs left is 12 minus the quantity 2 times the number x of omelets made: y = 12 - 2x.

#### Exercises

For each table, identify the independent and dependent variables. Represent the relationship using words, an equation, and a graph.

3. Paint in Can

4. Game Cost

Number of Chairs Painted, p	Paint Left (oz), L	Number of Snacks Purchased, s	Total Cost, C
0	128	0	\$18
1	98	1	\$21
2	68	2	\$24
3	38	3	\$27

#### 5. Elevation

Number of Flights of Stairs Climbed, n	0	1	2	3
Elevation (ft above sea level), E	311	326	341	356

## Quick Review

A nonlinear function is a function whose graph is not a line or part of a line.

## Example

The area A of a square field is a function of the side length s of the field. Is the function linear or nonlinear?

Side Length (ft), s	10	15	20	25
Area (ft2), A	100	225	400	625



#### Exercises

Graph the function shown by each table. Tell whether the function is linear or nonlinear.



7.

Х	Y
1	0
2	1
3	8
4	20

 X
 Y

 1
 0

 2
 4.5

 3
 9

 4
 13.5



9.





## **Quick Review**

A continuous graph is a graph that is unbroken. A discrete graph is composed of distinct, isolated points. In a realworld graph, show only points that make sense.

## Example

The total height h of a stack of cans is a function of the number n of layers of 4.5-in. cans used. This situation is represented by h = 4.5n. Graph the function.



## Exercises

Graph the function rule. Explain why the graph is continuous or discrete.

10. Walnuts Your cost c to buy w pounds of walnuts at 6/lb is represented by c = 6w.

11. **Moving** A truck originally held 24 chairs. You remove 2 chairs at a time. The number of chairs n remaining after you make t trips is represented by n = 24 - 2t.

12. Flood A burst pipe fills a basement with 37 in. of water. A pump empties the water at a rate of 1.5 in./h. The water level /, in inches, after t hours is represented by / = 37 - 1.5t.

13. Graph y = -|x| + 2.



## **Quick Review**

To write a function rule describing a real-world situation, it is often helpful to start with a verbal model of the situation.

## Example

At a bicycle motocross (BMX) track, you pay \$40 for a racing license plus \$15 per race. What is a function rule that represents your total cost?

total cost = license fee + fee per race \* # number of races

$$C = 40 + 15 \cdot r$$

A function rule is  $C = 40 + 15 \cdot r$ .

#### Exercises

Write a function rule to represent each situation.

14. **Landscaping** The volume V remaining in a 243-ft<sup>3</sup> pile of gravel decreases by 0.2 ft<sup>3</sup> with each shovelful s of gravel spread in a walkway.

15. **Design** Your total cost C for hiring a garden designer is \$200 for an initial consultation plus \$45 for each hour h the designer spends drawing plans.

## **Quick Review**

A relation pairs numbers in the domain with numbers in the range. A relation may or may not be a function.

#### Example

Is the relation {(0, 1), (3, 3), (4, 4), (0, 0)} a function?

The x-values of the ordered pairs form the domain, and the y-values form the range. The domain value 0 is paired with two range values, 1 and 0. So the relation is not a function.

# Exercises

Tell whether each relation is a function.

16.  $\{(-1, 7), (9, 4), (3, -2), (5, 3), (9, 1)\}$ 

17.  $\{(2, 5), (3, 5), (4, -4), (5, -4), (6, 8)\}$ 

Evaluate each function for x = 2 and x = 7.

18. 
$$f(x) = 2x - 8$$

19. h(x) = -4x + 61

